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# Comparative Study of Forced Oscillators for the Adaptive Generation of Rhythmic Movements in Robot Controllers

Melanie Jouaiti · Patrick Hénaff

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**Abstract** The interest of Central Pattern Generators (CPGs) in robot motor coordination is universally recognized so much so that a lot of possibilities on different scales of modeling are nowadays available. While each method obviously has its advantages and drawbacks, some could be more suitable for human-robot interactions.

In this paper, we compare three oscillator models: Matsuoka, Hopf and Rowat-Selverston models. These models are integrated to a control architecture for a robotic arm and evaluated in simulation during a simplified handshaking interaction which involves constrained rhythmic movements. Furthermore, Hebbian plasticity mechanisms are integrated to the Hopf and Rowat-Selverston models which can incorporate such mechanisms, contrary to the Matsuoka. Results show that the Matsuoka oscillator is subpar in all aspects and for the two others, that plasticity improves synchronization and leads to a significant decrease of the power consumption.

**Keywords** Oscillator · synchronization · rhythmic movements · robot controller

## 1 Introduction

Central Pattern Generators (CPGs) are biological structures found in the central nervous system of vertebrates or in some ganglia of invertebrates. CPGs

can generate a rhythmic signal even when the input signal is not rhythmic, modulated by afferent sensory feedbacks. While their implication in upper limb movements is strongly suspected (Schaal, 2006; Zehr et al, 2004), their role in locomotion has been recognized and widely studied. Mesoscopic CPGs are usually based on a pair of half-center neurons (Grillner and Wallen, 1985), controlling the extensor and flexor muscles. CPGs have several interpretations which differ according to the level of bio-inspiration (Ijspeert, 2008; Yu et al, 2014). Biologists usually present CPGs as complex structures which encompass sensory neurons, motor neurons and interneurons and receive sensory feedback (Rybak et al, 2006; Cattaert and Le Ray, 2001). However, in computational neuroscience, some aspects tend to not be taken into account for simplicity's sake. While some studies endeavour to be biologically accurate (Nassour et al, 2019; Taga et al, 1991; Manoonpong et al, 2008), others present simplified interpretations (Mori et al, 2004; Wu and Ma, 2010).

The interest of using CPGs in robotics is nowadays widely recognized, so much so that a great variety of possibilities has been proposed (see Yu et al (2014); Ijspeert (2008) for reviews). The term CPG refers to a network of coupled oscillators. Non-linear models of CPGs, composed of relaxation oscillators, can be entrained by an oscillatory input or with a coupled CPG if the coupling is strong enough or if the input frequency is close enough to the intrinsic frequency of the oscillator, thus ensuring coordination. Even though CPGs have mostly been used for robotic locomotion (Taga, 1995; Shan and Nagashima, 2002; Ayers, 2004; Kamimura et al, 2005; Arena et al, 2006; He et al, 2006; Pelc et al, 2008; Sprowitz et al, 2010; Liu et al, 2011; Pinto et al, 2012; Wang et al, 2013), see Ijspeert (2008) for a review,

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some studies explore how CPGs affect upper limb control as well (Williamson, 1998; Yang et al, 2010). The strength of CPGs resides in their self-synchronization ability, their oscillating stability despite perturbation and the variety of behaviors they can generate. Besides, plasticity mechanisms can be integrated, thus making the CPG even more robust and versatile. This is actually essential to have adaptive robot controllers.

In social, collaborative robotics, human-robot interactions are paramount. If humans are to be comfortable interacting with robots, robots have to behave in a coherent and adaptive way, i.e. their response has to be suited to the partner and the social context. Human interactions entail a lot of rhythmic non-verbal communication (waving, handshaking, walking) and it has been observed that humans learn from these interactions and adapt to their partner, thus leading to interpersonal synchronization and motor coordination and to a greater engagement in the interaction. It is hence important for robots to be able to replicate that. We consider the case of handshaking which is a highly social act responsible for the creation of conscious and unconscious links between the interaction partners. Despite its apparent triviality, it involves complex tasks from a neuroscience and robotics point of view, one of them being the emergence of synchronization and phase-locking observed during the act. Kasuga and Hashimoto (2005) introduced a framework for human-robot handshaking using neural oscillators. They were able to control how passive or active the robot handshake was and modulate the human perception of the response.

A great variety of oscillators can be found in the literature at different modeling scales; amongst the most popular, to name a few: microscopic (Hodgkin and Huxley, 1952) which models single neuron; mesoscopic (Rowat and Selverston, 1993; Matsuoka, 1985) which models populations of neurons, taking biological mechanisms into account and macroscopic (Hopf, 1942) which also models populations of neurons but with no bio-inspiration. To determine which oscillator is actually more suited to a given purpose and why, our contribution consists in comparing three oscillator models in the same control architecture (Kasuga and Hashimoto, 2005) and in explaining the differences observed. A similar endeavour was undertaken by Collins and Richmond (1994) who compared three different neuronal oscillator models (Stein, Van der Pol and Fitzhugh Nagumo) and two different coupling schemes for locomotion. They studied the ability of each oscillator to produce the walking, trotting, and bounding gaits, as well as the possibility to switch between multiple gait patterns. The originality of this paper resides in comparing three oscillators by

evaluating them on their entrainment abilities, power consumption with and without plasticity mechanisms in the same handshaking task, which, to our knowledge, has never been done before.

This paper is organized as follows. First, we present the three oscillator models studied: Matsuoka, Hopf and Rowat-Selverston. They were chosen because Matsuoka is a neural oscillator, Hopf a non-linear oscillator and they are both the most popular choices in robotics. Besides, we believe Rowat-Selverston to be a compromise between the two alternatives, being a non-linear oscillator inspired by Van der Pol but it also encompasses biological inspiration, making it a neural oscillator as well. Then, in section III, we compare the three oscillators, in one set of experiments on their entrainment range and in another set of experiments with their synchronization capacity. Then we integrate plasticity mechanisms to Hopf and Rowat-Selverston and evaluate the energetic cost. Finally, in section IV, we discuss our results and future prospects.

## 2 Material and Method

### 2.1 Oscillating Neuron Models

#### 2.1.1 Matsuoka neuron

Introduced in 1985, the Matsuoka model (Matsuoka, 1985) is undoubtedly the most well-known and employed neural oscillator. In the original paper, a single neuron defined by two differential equations was studied, as well as its behaviour in networks of  $n$  coupled neurons. Since Taga et al (1991), it has become customary to couple two neurons in CPGs. While this model has mostly been used for robotic biped locomotion (Liu et al, 2006, 2007, 2008; Panwart and Kumar, 2012; Liu et al, 2012; Al-Busaidi et al, 2012), some original works applied it to achieve human-robot handshaking (Kasuga and Hashimoto, 2005), a chewing robot (Xu et al, 2009) or traffic lights regulation (Fang et al, 2013). A Matsuoka neuron is a mesoscopic model defined by the following equations:

$$\dot{x} = \frac{1}{T}(-x - bv + c + \epsilon F) \quad (1a)$$

$$\dot{v} = \frac{1}{\tau}(-v + y) \quad (1b)$$

$$y = \max(x, 0) \quad (1c)$$

where  $F$  represents the input signal,  $T$  and  $\tau$  are time constants and  $b$  the self-inhibition (or neuron fatigue),  $y$  is the cell output and  $c$  the excitatory tonic input.

### 2.1.2 Hopf oscillator

The non-linear Hopf oscillator (Hopf, 1942) is particularly popular in robotics. It has been widely applied to robot locomotion (Li et al, 2013; Matos and Santos, 2010; Ijspeert, 2004; Brambilla et al, 2006; Fuente et al, 2013; Buchli and Ijspeert, 2008; Righetti and Ijspeert, 2006, 2008) and robot swimming (Seo et al, 2010; Hu et al, 2011; Zhou and Low, 2012; Hu et al, 2014); but also to robot hopping (Buchli et al, 2005, 2006), drumming (Degallier et al, 2006), crawling, reaching (Degallier et al, 2008), the flight of a robotic bat (Chung and Dorothy, 2010).

The Hopf oscillator can be considered as a macroscopic model of neural oscillator structures, so it does not have the half center structure usually present in neural oscillators. The equations for a Hopf cell are defined as follows:

$$\dot{x} = (\mu - (x^2 + y^2))x - \theta y + \epsilon F \quad (2a)$$

$$\dot{y} = (\mu - (x^2 + y^2))y + \theta x \quad (2b)$$

with  $F$  the input signal and  $y$  the neuron output. For  $\mu < 0.5$ , oscillations are damped.  $\mu$  determines the output amplitude which can be influenced by  $\epsilon$  the input gain.  $\theta$  determines the intrinsic frequency of the oscillator ( $\omega \approx 0.155 \cdot \theta$ ).

### 2.1.3 Rowat-Selverston *Neuron*

The Rowat-Selverston neuron (Rowat and Selverston, 1993) is able to produce discrete and rhythmic activities depending of two parameters like shown in Jouaiti and Henaff (2018); Nassour et al (2014). Properties of the Van der Pol can be applied to it since it is a generalized Van der Pol oscillator, notably the dynamic Hebbian learning of frequency introduced by Righetti et al (2006), as demonstrated in Jouaiti et al (2018). This model has been underused to this day, only few studies employ it (e.g. (Jouaiti et al, 2018; Arian and Irfanoglu, 2011; Nassour et al, 2014)).

$$\dot{V} = y + \epsilon F \quad (3a)$$

$$\dot{y} = \frac{1}{\tau_m} \left( \sigma_f - \frac{\tau_m}{\tau_s} - 1 - \sigma_f \tanh^2 \left( \frac{\sigma_f}{A_f} V \right) \right) y - \frac{1 + \sigma_s}{\tau_s \tau_m} V + \frac{A_f}{\tau_s \tau_m} \tanh \left( \frac{\sigma_f}{A_f} V \right) \quad (3b)$$

with  $F$  the input signal and  $y$  the neuron output,  $V$  the cellular membrane potential,  $q$  the slow current,  $\tau_m$  the time constant of the cellular membrane,  $\tau_s$  is the time constant of slow current activation ( $\tau_m \ll \tau_s$ ),  $\sigma_s$  and

$\sigma_f$  represent respectively the conductance of slow and fast currents,  $A_f$  influences the amplitude of  $V$ .

### 2.1.4 Mathematical Plasticity Modeling

Righetti et al (2006) presented a frequency adaptation rule for the Hopf oscillator. This rule allows the oscillator to learn the input frequency and truly adapt to the input signal. Besides, when the interaction stops, the system retains the learning and remains at the learned frequency:

$$\dot{\theta} = -\eta \frac{y}{\sqrt{x^2 + y^2}} F \quad (4)$$

With  $\eta$  the learning step.

For the Rowat-Selverston cells, the plasticity mechanisms previously introduced in Jouaiti et al (2018) are employed: frequency learning, amplitude learning and synaptic gain learning:

$$\dot{\sigma}_s = 2\epsilon F \sqrt{\tau_m \tau_s (1 + \sigma_s - \sigma_f)} \cdot \frac{y}{\sqrt{V^2 + y^2}} \quad (5)$$

$$\dot{A}_f = -\mu \left( \left( \frac{\nu \sigma_f V}{A_f} \right)^2 - F^2 \right) \quad (6)$$

$$\dot{\epsilon} = \lambda \tanh^2(\xi F) (1 - (\epsilon F)^2) \quad (7)$$

with  $\mu$  and  $\lambda$  learning steps,  $\nu$  a gain modulating the output amplitude and  $\xi$  a gain ensuring that  $\tanh^2(\xi F)$  is 0 when no input is applied and 1 otherwise.

For the Matsuoka model, one could modulate the global output as done in Taga et al (1991) or change the time constants (de Rugy et al, 2003). We will present the latter option. This method consists in comparing the oscillator period  $P_r$  and the target period  $P_t$  and if this difference exceeds a given threshold  $\delta$ , the following adaptation equation is enabled:

$$\tau = c_1 \cdot P_t \quad (8)$$

$$T = c_2 \cdot P_t \quad (9)$$

with  $c_1$  and  $c_2$  two empirically determined constants and  $P_t$  the target period, i.e. the period of the input.

### 2.1.5 Parameter Tuning

The intrinsic properties of each oscillator model can be modulated thanks to the various parameters available. Properties of interest are the intrinsic frequency and amplitude of the oscillations.

For the Matsuoka model, the amplitude is determined by  $c$ , though this is merely an offset so the amplitude really does not change. For Hopf and Rowat-Selverston,  $\mu$  and  $A_f$  determine the amplitude respectively but it can be further influenced by the input amplitude  $\epsilon F$ . Note though that setting the amplitude of Hopf is rather troublesome and some output amplitudes are just impossible to set, Rowat-Selverston is more straightforward because the amplitude is proportional to  $A_f$ .

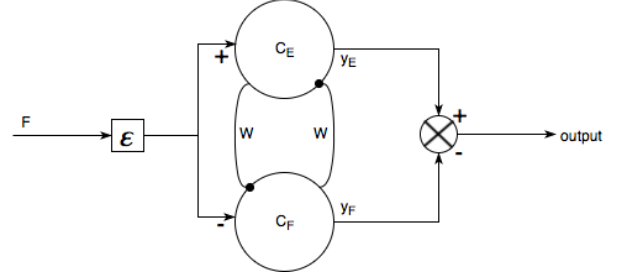
In the Matsuoka model, four parameters are necessary to set the intrinsic frequency  $\left(\omega = \frac{1}{\tau} \sqrt{\frac{(T+\tau)b}{T \cdot W} - 1}\right)$  and two conditions have to be met in order to obtain oscillations ( $W > 1 + T/\tau$  and  $b > W + 1$ ) (see Matsuoka (2011) for details). Note also that Matsuoka synchronizes better with an input signal when it is unable to oscillate by itself. For Hopf, if  $\mu < 0.5$ , the oscillations are damped; the intrinsic frequency depends solely on  $\theta$ . Finally, the Rowat-Selverston model produces oscillations if  $\sigma_f > 1 + \tau_m/\tau_s$ . The intrinsic frequency is dependent on  $\tau_m$ ,  $\tau_s$ ,  $\sigma_s$ ,  $W$ . While the Rowat-Selverston model seems as difficult to control as the Matsuoka model, it really is not so. Setting a particular intrinsic frequency is, in both cases, a complicated endeavour but putting the oscillator in conditions such that it can adapt to a wide range of frequencies is actually fairly easy with Rowat-Selverston. Indeed, by choosing wisely  $\tau_m$  and  $\tau_s$ , the oscillator can cover the desired frequency range quite easily, even if it is quite wide. Then the value of  $\sigma_s$  hardly matters, thanks to the learning rule. On the contrary, in order to change the frequency range of the Matsuoka model, the time constants have to be changed since they're only able to cover a small range. In biological systems, the membrane time constants are set and cannot be modulated so this kind of plasticity is not biologically sound.

## 2.2 Implementing the CPG controller for a robot

### 2.2.1 Coupling the oscillatory neurons

From now on, we consider two coupled oscillators controlling the flexor and the extensor muscles in reference to the half center structure introduced by Rybak et al (2006). However, in robotics, this is hardly applicable as such since robots have a single joint in place for the flexor and extensor parts. It is then common practice to subtract both commands to obtain the output (see Figure 1).

In all equations, the term in  $W$  models the mutual inhibition between the extensor and the flexor cells.



**Fig. 1** Coupled oscillatory cells.  $C_{\{E,F\}}$  indicates whether the neuron cell controls the extensor or the flexor

The equations are thus rewritten as follows (with  $F_F = -F_E$ ):

#### • Matsuoka model

$$\dot{x}_{\{E,F\}} = \frac{1}{T} (-x_{\{E,F\}} - W \cdot y_{\{F,E\}} - b \cdot v_{\{E,F\}} + c + \epsilon F_{\{E,F\}}) \quad (10a)$$

$$\dot{v}_{\{E,F\}} = \frac{1}{\tau} (-v_{\{E,F\}} + y_{\{E,F\}}) \quad (10b)$$

$$y_{\{E,F\}} = \max(x_{\{E,F\}}, 0) \quad (10c)$$

#### • Hopf model

$$\dot{x}_{\{E,F\}} = (\mu - (x_{\{E,F\}}^2 + y_{\{E,F\}}^2))x_{\{E,F\}} - W \tanh(x_{\{F,E\}}) - \theta y_{\{E,F\}} + \epsilon F_{\{E,F\}} \quad (11a)$$

$$\dot{y}_{\{E,F\}} = (\mu - (x_{\{E,F\}}^2 + y_{\{E,F\}}^2))y_{\{E,F\}} + \theta x_{\{E,F\}} \quad (11b)$$

Note that the term  $W \tanh(x_j)$  has been added to the original model in order to couple the two Hopf cells and thus obtain a half center model. In the rest of the paper, we consider  $W = 1$  for Hopf.

#### • Rowat-Selverston model

$$\dot{V}_{\{E,F\}} = y_{\{E,F\}} - W \frac{y_{\{E,F\}}}{1 + e^{-4y_{\{F,E\}}}} + \epsilon F_{\{E,F\}} \quad (12a)$$

$$\dot{y}_{\{E,F\}} = \frac{1}{\tau_m} \left( \sigma_f - \frac{\tau_m}{\tau_s} - 1 - \sigma_f \tanh^2 \left( \frac{\sigma_f}{A_f} V_{\{E,F\}} \right) \right) y_{\{E,F\}} - \frac{1 + \sigma_s}{\tau_s \tau_m} V_{\{E,F\}} + \frac{A_f}{\tau_s \tau_m} \tanh \left( \frac{\sigma_f}{A_f} V_{\{E,F\}} \right) \quad (12b)$$

### 2.2.2 The Kasuga Control Architecture

Kasuga and Hashimoto (2005) introduced a control architecture for human-robot handshaking using

Matsuoka neurons. This framework was validated in simulation and experimentally. This architecture controls two robot joints which are coupled together (see Figure 2). The input of each neural oscillator is the weighted sum of the force exerted on the joint, absolute value of the force and output of the other joint controller. The force inputs determine the oscillation amplitude and whether the handshake is passive or active. Coupling the two joints together prevents the amplitude from decreasing, which has been observed with the Matsuoka oscillator by Kasuga and Hashimoto (2005). The output is considered as an angular velocity command.

In this system, the torque is applied by the ball to the gripper, which in turns entrains the robot joints and thus provides the CPG inputs. Because of the mechanical coupling, they form a closed loop with the human partner.

In order to integrate the oscillators into the Kasuga architecture for joints  $i$  and  $j$ , the cells equations become:

#### • Matsuoka model

$$\begin{aligned} \dot{x}_{i\{E,F\}} = & \frac{1}{T}(-x_{i\{E,F\}} - W \cdot y_{i\{F,E\}} - b \cdot v_{i\{E,F\}} + c) \\ & + L_{i2}F_{i\{E,F\}} + L_{i1}|F_{i\{E,F\}}| + \\ & K_{i\{E,F\}}(y_{jE} - y_{jF}) \end{aligned} \quad (13a)$$

$$\dot{v}_{i\{E,F\}} = \frac{1}{\tau}(-v_{i\{E,F\}} + y_{i\{E,F\}}) \quad (13b)$$

$$y_{i\{E,F\}} = \max(x_{i\{E,F\}}, 0) \quad (13c)$$

With  $F_{iE} = -F_{iF}$ ,  $K_{iE} = -K_{iF}$  and  $j$  the other joint.

#### • Hopf model

$$\begin{aligned} \dot{x}_{i\{E,F\}} = & (\mu - (x_{i\{E,F\}}^2 + y_{i\{E,F\}}^2))x_{i\{E,F\}} \\ & - \tanh(x_{i\{E,F\}}) - \theta_i y_{i\{E,F\}} + \\ & L_{i2}F_{i\{E,F\}} + L_{i1}|F_{i\{E,F\}}| + \\ & K_{i\{E,F\}}(x_{jE} - x_{jF}) \end{aligned} \quad (14a)$$

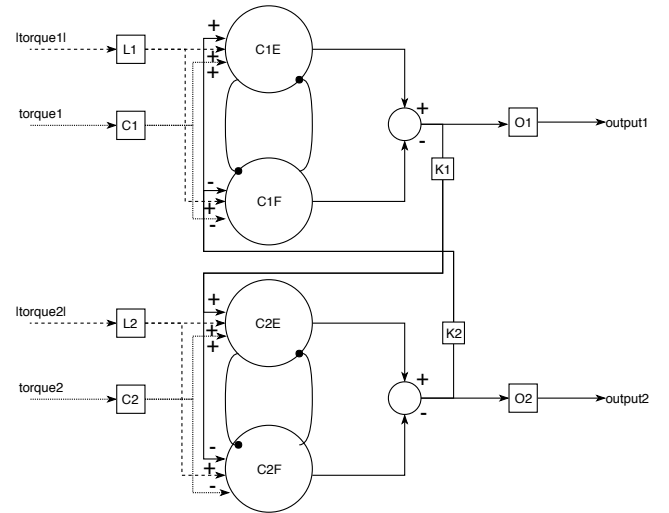
$$\begin{aligned} \dot{y}_{i\{E,F\}} = & (\mu - (x_{i\{E,F\}}^2 + y_{i\{E,F\}}^2))y_{i\{E,F\}} + \\ & \theta_i x_{i\{E,F\}} \end{aligned} \quad (14b)$$

#### • Rowat-Selverston model

$$\begin{aligned} \dot{V}_{i\{E,F\}} = & y_{i\{E,F\}} - W \frac{y_{i\{E,F\}}}{1 + e^{-4y_{i\{E,F\}}}} + \\ & \cdot L_{i2}F_{i\{E,F\}} + L_{i1}|F_{i\{E,F\}}| + \end{aligned} \quad (15a)$$

$$\begin{aligned} \dot{y}_{i\{E,F\}} = & \frac{1}{\tau_m} \left( \sigma_f - \frac{\tau_m}{\tau_s} - 1 - \right. \\ & \left. \sigma_f \tanh^2 \left( \frac{\sigma_f}{A_{fi}} V_{i\{E,F\}} \right) \right) y_{i\{E,F\}} - \\ & \frac{1 + \sigma_s}{\tau_s \tau_m} V_{i\{E,F\}} + \\ & \frac{A_{fi\{E,F\}}}{\tau_s \tau_m} \tanh \left( \frac{\sigma_f}{A_{fi\{E,F\}}} V_{i\{E,F\}} \right) \end{aligned} \quad (15b)$$

Unless stated otherwise, the various gains are:  $O_i = 0.2$ ,  $K_i = 0.5$ ,  $L_{i2} = 0.4$ ,  $L_{i1} = 0.5$  for Rowat-Selverston and Hopf oscillators. For the Matsuoka oscillator, the input gains differ:  $L_{i2} = 0.02$ ,  $L_{i1} = 0.035$ . Those values were obtained empirically. One important criterion was that the ball should stay inside the gripper. Indeed, some parameters created instability and unpredictable behavior from the robot. Then, the parameters were fine-tuned to try and get the best possible performance.



**Fig. 2** Oscillatory cells integrated to the generalized Kasuga architecture.  $C_i$ ,  $L_i$ ,  $K_i$ ,  $O_i$  are gains and  $C_{i\{E,F\}}$  the neuron cell for the joint  $i$  controlling the extensor or flexor

#### 2.3 Evaluation of coordination: Phase Locking Value

Introduced by Lachaux et al (1999) to measure coordination in brain signals, the Phase Locking Value (PLV) assumes that the two signals are locked with a constant phase difference. Allowing for deviations, it evaluates

this spread: from 0 (no coordination) to 1 (perfect coordination). We use a variation of the original implementation. First, one has to obtain the instantaneous phase  $\phi$  with the Hilbert transform, then the instantaneous PLV can be computed:

$$PLV(t) = \frac{1}{N} \left| \sum_{i=0}^N e^{j(\phi_1(i) - \phi_2(i))} \right| \quad (16)$$

with  $N$  the sliding window size,  $j = \sqrt{-1}$ ,  $\phi_k$  the instantaneous phase of signal  $k$ .

### 3 Results: Comparison between three oscillator models

The three oscillators are evaluated according to their entrainment range and their synchronization capacity during a handshaking simulation inspired by Kasuga and Hashimoto (2005). Then Hebbian plasticity is integrated to the Hopf and Rowat-Selverston models and the impact on the energetic cost is observed. We also implement a constants adaptation mechanism for Matsuoka.

#### 3.1 Entrainment Performance

In order to determine their entrainment range, each oscillator model is subjected to various input frequencies for 100 s. At the beginning, the input frequency is low at 0.1 Hz and increases by 0.1 every 100 s. At each frequency change, the average PLV is computed between the input and output values of the oscillator, taking only the last 100 s into account. If this value is below 0.95, the input frequency is considered outside the bandwidth of the oscillator.

The process is repeated for several intrinsic frequencies of the oscillators. Since the intrinsic frequency depends on the parameters, they are tuned in order to get matching frequencies:  $\sigma_s$ ,  $\theta$  and  $b$  for Rowat-Selverston, Hopf and Matsuoka respectively.

Table 1 shows the entrainment range of each model for various intrinsic frequencies. We can clearly observe that the Matsuoka model is very limited and is not able to synchronize if the input frequency differs too much from its own. Besides, Rowat-Selverston cannot synchronize if the input frequency is too low, contrary to Hopf, but its frequency range is considerably larger.

Note that the entrainment capacity  $\Delta\omega$  of Hopf is highly dependent on the value of  $\epsilon$ . The stronger the

coupling, i.e the higher  $\epsilon$ , the better the oscillator synchronizes. On the contrary,  $\epsilon$  has to be small for Matsuoka and neither too small, nor too big for Rowat-Selverston. Due to those discrepancies, we did not employ the same  $\epsilon$  value for the oscillators but rather chose to put them all in the best possible synchronization conditions which were determined by running simulations with an extensive range of values of  $\epsilon$ , we then selected the value of  $\epsilon$  which yielded the higher PLV score.

**Table 1** The entrainment range where  $PLV \geq 0.95$  for each oscillator with following parameters: Rowat-Selverston parameters:  $\tau_m = 0.35$ ,  $\tau_s = 3.5$ ,  $\sigma_f = 1.0$ ,  $W = 0.05$ ,  $\epsilon = 0.1$ ,  $A_f = 0.5$ . Hopf parameters:  $\mu = 0.5$ ,  $\epsilon = 1.0$ . Matsuoka parameters:  $\tau = 0.5$ ,  $T = 0.25$ ,  $\epsilon = 0.001$ ,  $c = 0.1$ ,  $A = 3$ .  $\omega_{intr}$  is the intrinsic frequency of the neuron determined by  $\sigma_s$ ,  $\theta$  and  $b$  respectively

| Model            |            | $\omega_{intr}$<br>[Hz] | $\omega_{min}$<br>[Hz] | $\omega_{max}$<br>[Hz] | $\Delta\omega =$<br>$\omega_{max} - \omega_{min}$ |
|------------------|------------|-------------------------|------------------------|------------------------|---|
|                  | $\sigma_s$ |                         |                        |                        |   |
| Rowat-Selverston | 13         | 0.5                     | 0.1                    | 13.8                   | 13.7  |
|                  | 50         | 1.0                     | 0.1                    | 18.3                   | 18.2  |
|                  | 120        | 1.5                     | 0.2                    | 23.7                   | 23.5  |
|                  | 200        | 2.0                     | 0.2                    | 28.9                   | 28.7  |
|                  | 340        | 2.5                     | 0.3                    | 36.9                   | 36.6  |
|                  | 490        | 3.0                     | 0.3                    | 45.5                   | 45.2  |
|                  | $\theta$   |                         |                        |                        |   |
| Hopf             | 3.5        | 0.5                     | 0.1                    | 9.5                    | 9.4   |
|                  | 7          | 1.0                     | 0.1                    | 9.8                    | 9.7   |
|                  | 10         | 1.5                     | 0.1                    | 10.0                   | 9.9   |
|                  | 14         | 2.0                     | 0.1                    | 10.3                   | 10.2  |
|                  | 16         | 2.5                     | 0.1                    | 10.5                   | 10.4  |
|                  | 20         | 3.0                     | 0.1                    | 10.8                   | 10.7  |
|                  | $b$        |                         |                        |                        |   |
| Matsuoka         | 3.5        | 0.5                     | 0.4                    | 0.7                    | 0.3   |
|                  | 8          | 1.0                     | 0.9                    | 1.2                    | 0.3   |
|                  | 13         | 1.5                     | 1.3                    | 1.6                    | 0.3   |

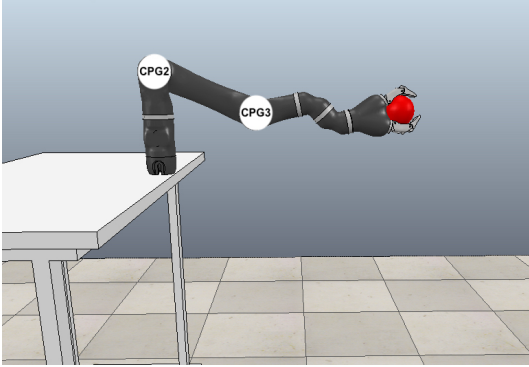
#### 3.2 Synchronization Evaluation in Simulated Handshaking

In this section, in order to evaluate the three oscillators, they are placed into the version of the Kasuga architecture introduced previously in section 2.2.2, which has been generalized such that any oscillator can be integrated.

The simulations have been conducted with the Kinova Mico robot in the V-REP simulator. Since grasping cannot accurately be simulated, we realize a oversimplified handshake with a static collidable ball instead of the human hand. The ball is animated with an up and down motion of amplitude 0.16 m and frequency 2 Hz, unless stated otherwise. The 2 Hz frequency was found appropriate for handshaking (Tagne et al, 2016). The moving ball forces the arm to move along, by ex-



erting a force on the fingers of the robot (see Figure 3).



**Fig. 3** Simulated robotic arm with the static ball inside its gripper. We control the ball kinematics. We consider a rigid mechanical link because we want to impose a force on the robot which cannot be influenced. We set the ball position repeatedly according to a sinusoidal signal. The time step is small enough so that the motion appears smooth

The Mico arm has six degrees of freedom, but in the current setup, inspired by Kasuga and Hashimoto (2005), two joints, only the shoulder and elbow (joints 2 and 3 of the Mico robot) are controlled, the four other joints are locked. At the beginning of the simulation, the robot is not subjected to any external force (other than gravity). Then, the ball moves in the vertical plane, applying a perturbation to the robotic arm. Finally, the interaction stops and the ball is released.

In order to evaluate how the oscillators react when subjected to various frequency changes, the input signal applied to the ball varies across time: from  $t = 0$  s to  $t = 20$  s, 0.5 Hz; from  $t = 20$  s to  $t = 40$  s, 1.0 Hz; from  $t = 40$  s to  $t = 60$  s, 1.5 Hz; from  $t = 60$  s to  $t = 80$  s, 2.0 Hz; from  $t = 80$  s to  $t = 100$  s, 1.5 Hz; at  $t = 100$  s, the ball is released and until  $t = 110$  s, no force is applied.

### 3.2.1 Results without any Plasticity Mechanisms

At the beginning of the interaction, the intrinsic frequency of each oscillator is 1 Hz. See Table 2 for the parameters used in the simulations.

**Table 2** Oscillator parameters.

| Model            | Parameters   |
|------------------|--|
| Matsuoka         | $\tau = 0.5$ , $T = 0.25$ , $c = 0.1$ ,<br>$W = 4.0$ , $b = 10.0$  |
| Rowat-Selverston | $\tau_m = 0.2$ , $\tau_s = 2.0$ , $\sigma_f = 1.0$ , $W = 0.05$ ,<br>$A_{f_2} = 0.5$ , $A_{f_3} = 0.9$ , $\sigma_s = 20$ |
| Hopf             | $\mu = 0.5$ , $\theta = 7.0$   |

Figures 4, 5 and 6 represent the CPG input and output over 3 s for each frequency range. Matsuoka appears unable to synchronize at 0.5 Hz and the motion is irregular during the whole simulation (Figure 4). Kasuga and Hashimoto (2005)'s results had a smooth and regular motion because the oscillator was put in a non-oscillating mode where the Matsuoka oscillator synchronizes better. Hopf and Rowat-Selverston, however, have satisfactory frequency entrainment and the motion is regular, except for 0.5 Hz where Hopf struggles to synchronize (Figure 5). For the three oscillators, we can also observe that the input signal slightly precedes the output signal.

The PLV, represented on Figure 7 is used to evaluate the coordination between the force exerted on the joints and each neural oscillator model. This confirms what we previously observed: while the Matsuoka PLV (mean PLV: 0.91, 0.86) appears satisfactory, it actually never reaches 1.0 and is highly irregular for 0.5 Hz. This can be explained by the fact that the PLV quality and accuracy decrease when the signals are not perfectly sinusoidal. The PLV of Rowat-Selverston (0.93, 0.93) is more regular than Hopf (0.91, 0.9) for 0.5 Hz, their performances are similar for the rest of the simulation, though the transitions are more noticeable for Rowat-Selverston.

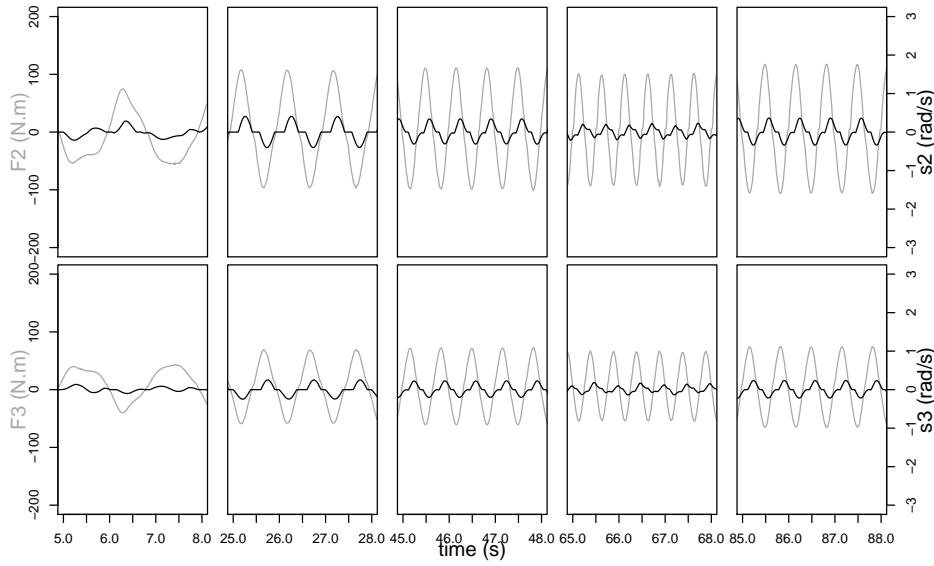
### 3.2.2 Results with Plasticity Mechanisms

In this section, Hebbian plasticity mechanisms are integrated to Hopf and Rowat-Selverston in order to have more adaptable and versatile systems. For Matsuoka, a time constants adaptation mechanism is implemented. Then, the oscillators are once more evaluated.

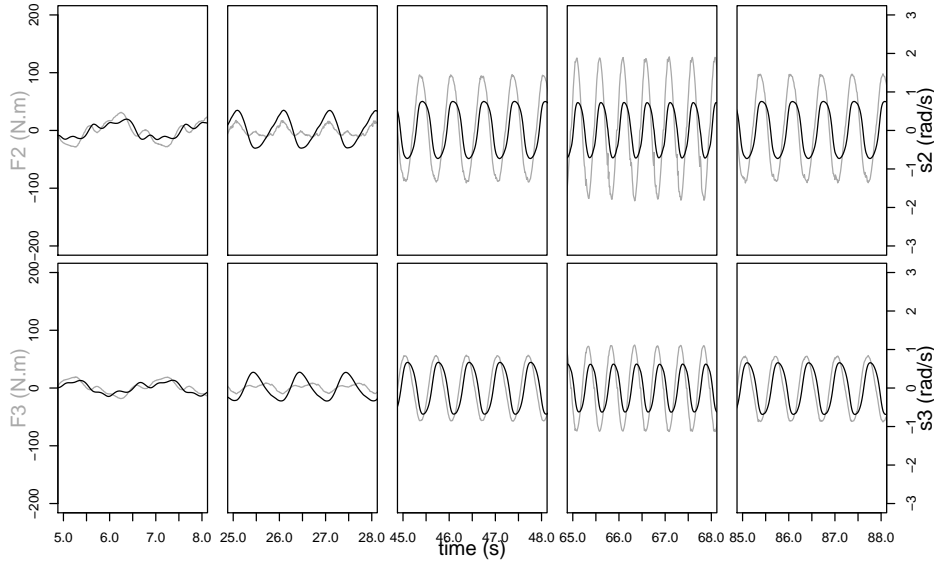
Simulations were run with the same parameters as previously. Additionally, for Rowat-Selverston,  $\lambda = 0.005$ ,  $\mu = 5e^{-6}$ ;  $\epsilon_2 = 0.2$ ,  $\epsilon_3 = 0.3$  and for Hopf,  $\eta_2 = 0.2$ ,  $\eta_3 = 0.25$ . Besides, plasticity could not be applied with the previous Kasuga parameters,  $L_{i1}$  had to be set to zero. For Matsuoka,  $C_i = 0.08$  and  $K_i = 0.1$ .

Figures 8, 9, 10 and 11 represent the CPG input and output over 3 s for each frequency range. Plasticity has little effect on the PLV (see Figure 12). The Matsuoka PLV (mean PLV: 0.86, 0.84) still never reaches 1.0 and is highly irregular for 0.5 Hz and 1 Hz. Rowat-Selverston with frequency learning (0.93, 0.92) and all plasticities (0.92, 0.89) is similar to Hopf (0.90, 0.89) overall. The PLV appears to decrease for joint 3 with Rowat-Selverston with plasticities, however, this can be explained by the fact that the force decreases so much, it becomes mostly noise, which the PLV does not handle well.





**Figure 4** Response of the Matsuoka oscillator. In gray: CPG input, in black: CPG output for both joints

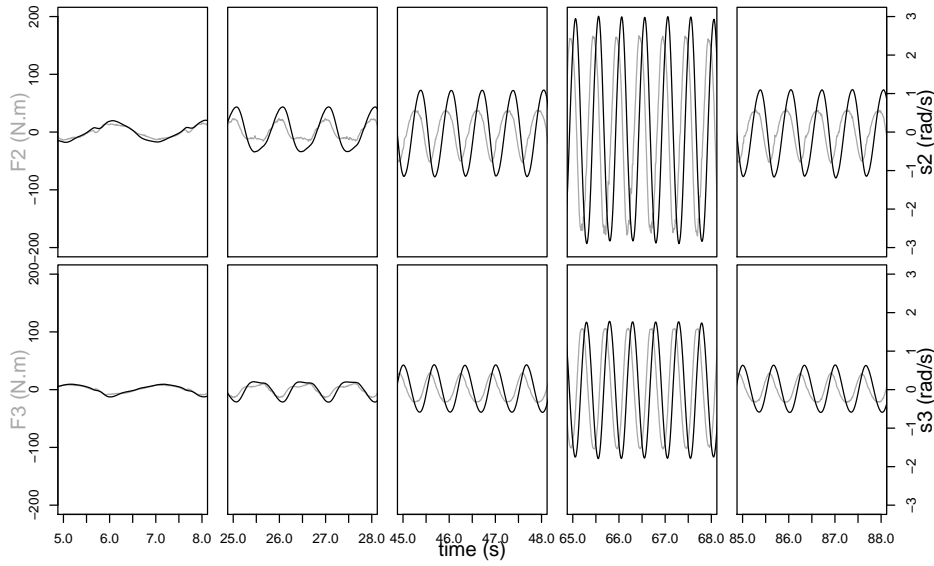


**Figure 5** Response of the Hopf oscillator. In gray: CPG input, in black: CPG output for both joints

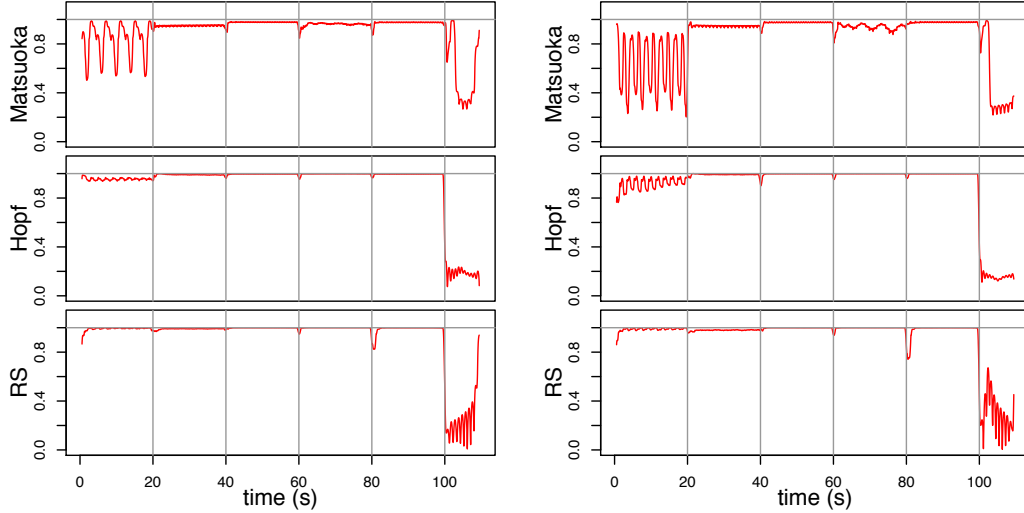
However, plasticity slightly extends the entrainment range (see Table 3), especially for Matsuoka which now has an entrainment range similar to Hopf. Furthermore it particularly improves the energetic impact of the oscillator. Indeed, if the intrinsic properties (amplitude, intrinsic frequency) of the oscillator are able to adapt to a varying input by learning more suitable parameters, the ball will be able to *anticipate* the input signal and will not exert so much force on the robotic arm and hence the amplitude of the force applied would be less important. This anticipation is evidenced by the fact that the delay between the input and output has now disappeared for Hopf and Rowat-Silverston. It is however still present

for Matsuoka. Table 4 shows that frequency learning already leads to a significant decrease of the average power consumed by the robot for all three oscillators. Furthermore,  $A_f$  and  $\epsilon$  learning for Rowat-Silverston decrease this consumption further.

Comparing with the simulations without plasticity, we see that the force applied on the joints for the three oscillators without plasticity never decreased. This shows that while the oscillator seems to adapt, it merely moves along, entrained by the ball, hence the delay between the input and output. This is further illustrated by the fact that once the interaction is over, the oscillator does not retain the ball frequency but returns to its own. On the other hand, for the oscillators endowed with plasticity, once they adapt



**Figure 6** Response of the Rowat-Silverston oscillator. In gray: CPG input, in black: CPG output for both joints



**Figure 7** PLV for joint 2 (left), joint 3 (right). The vertical grey lines delimit each frequency range. The horizontal line indicates the reference for perfect coordination at 1.0

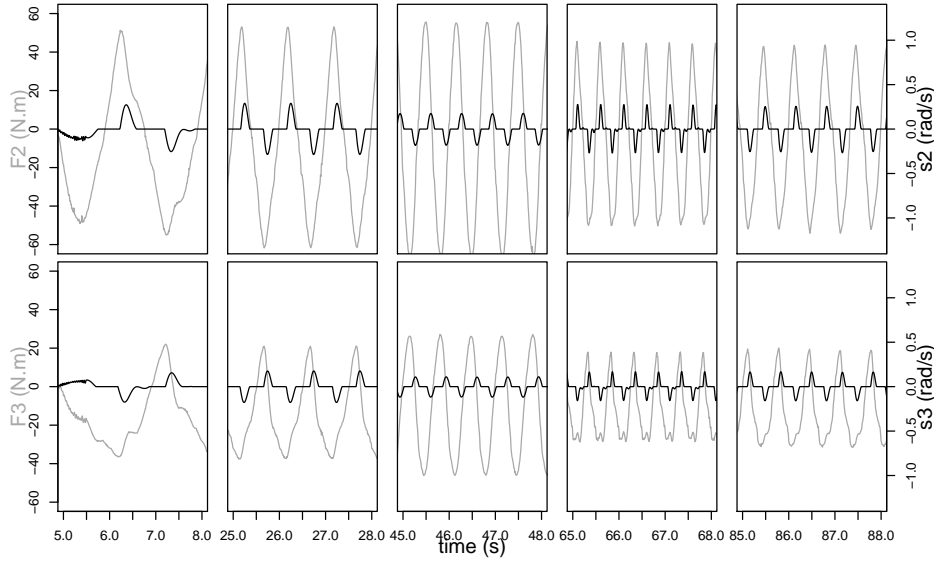
(new frequency learned), the delay disappears and a decrease in force can be observed, even more so for the Rowat-Silverston oscillator with all plasticities.

#### 4 Discussion

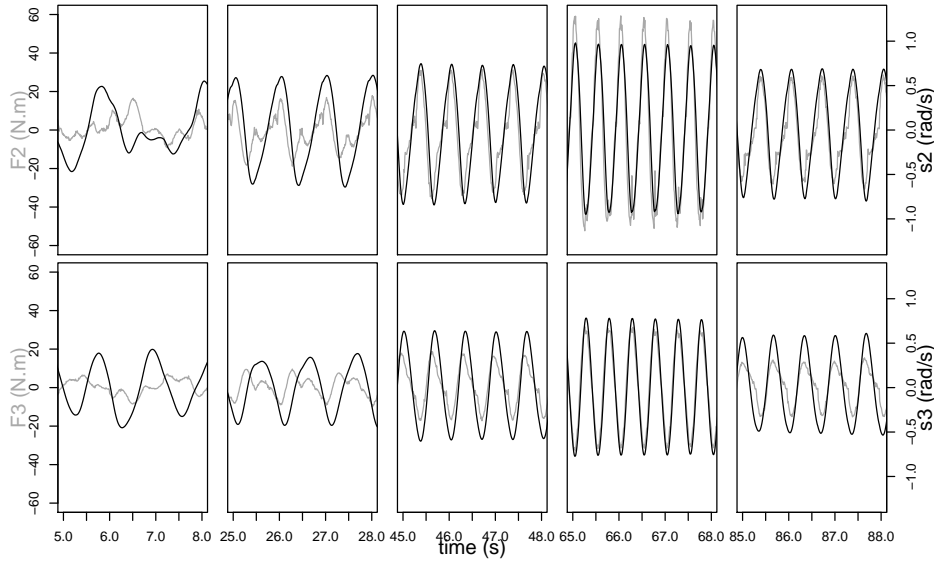
In this paper, we compared three oscillators often used in CPG modeling: Matsuoka, Hopf and Rowat-Silverston. These oscillators were evaluated firstly on their entrainment range. Then they were integrated into a simple control architecture and we compared their synchronization and power consumption performance with and without plasticity using a handshaking simulation.

We showed that integrating plasticity mechanisms into the three oscillators has no real impact on coordination performance but can lead to a significant power consumption decrease and an extended entrainment range.

With a cumbersome parameter tuning process, a very limited entrainment range, the Matsuoka oscillator is not the best choice for the adaptive control of a robot confronted to unpredictable feedbacks. Indeed, one has to bear in mind that CPG use is not restricted to human handshaking. To get good performance with the Matsuoka oscillator one has to have a rather accurate idea of the input (frequency, amplitude) beforehand. However, the time constants adaptation mechanism significantly improves the entrainment of this oscillator and even the power consumption.



**Figure 8** Response of the Matsuoka oscillator with time constants adaptation. In gray: CPG input, in black: CPG output for both joints



**Figure 9** Response of the Hopf oscillator with Frequency Learning. In gray: CPG input, in black: CPG output for both joints

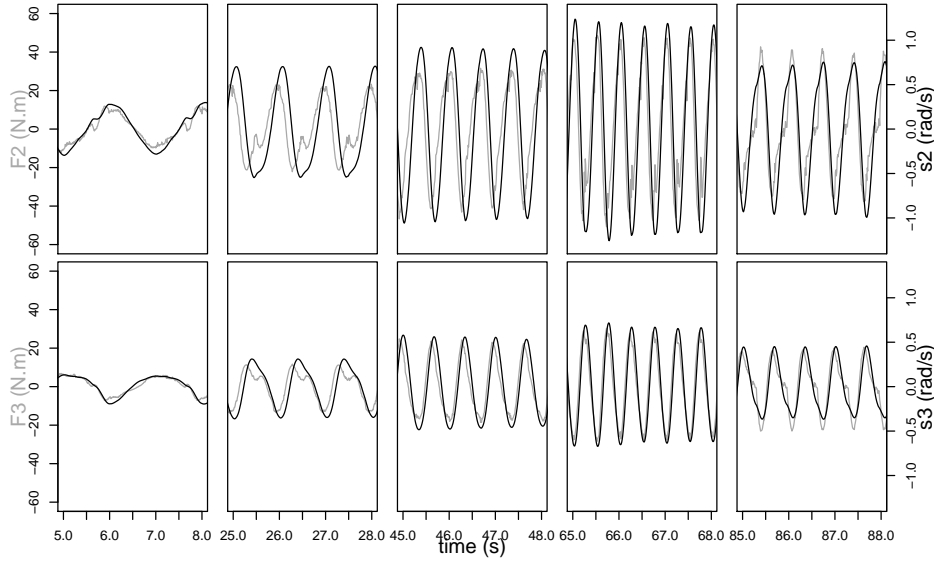
Comparing Hopf and Rowat-Selverston is however less straightforward. While Hopf synchronizes as well (sometimes better) as Rowat-Selverston and appears easier to control, this simplicity makes it less than obvious to render Hopf more adaptive by integrating new plasticity rules. Its entrainment range is noticeably smaller, even with frequency learning and its power consumption greater than Rowat-Selverston. It could probably benefit from amplitude learning however, amplitude setting is done in such a way that we fail to see how it could possibly be learned.

On the other hand, Rowat-Selverston is obviously more complex with more parameters to handle but it

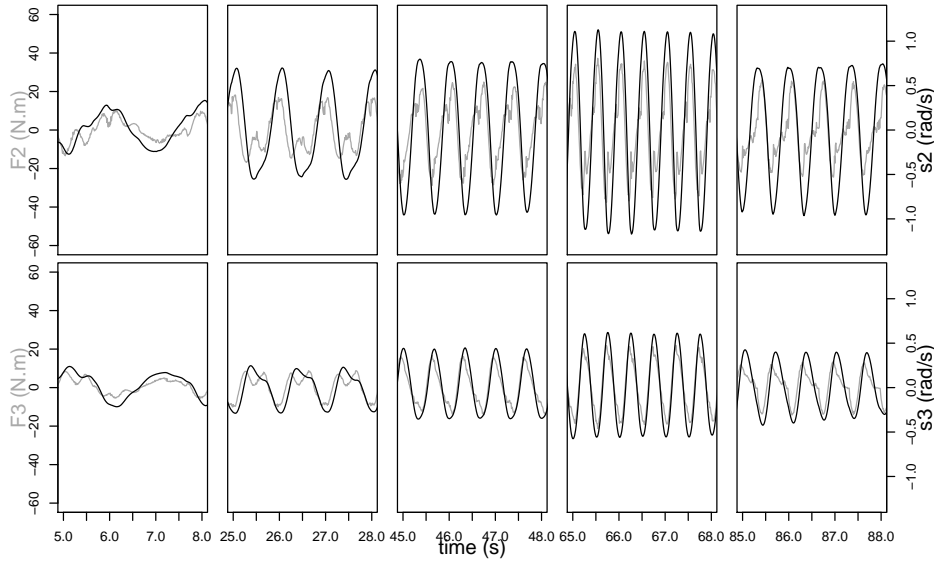
offers more flexibility and versatility, making it possible to design plasticity mechanisms allowing the system to truly adapt and not only offer a wide entrainment range but also a significantly lower power consumption.

Furthermore, the three oscillators are all non-linear systems, however the degree of non-linearity can be modified more easily for Rowat-Selverston and Hopf than Matsuoka. Rowat-Selverston also has a discrete mode where it behaves like a PID controller (Jouaiti and Hénaff, 2018). This, however, does not seem to be possible for Hopf and Matsuoka.

We feel that this study can help understand these oscillators better and for which purpose they are better



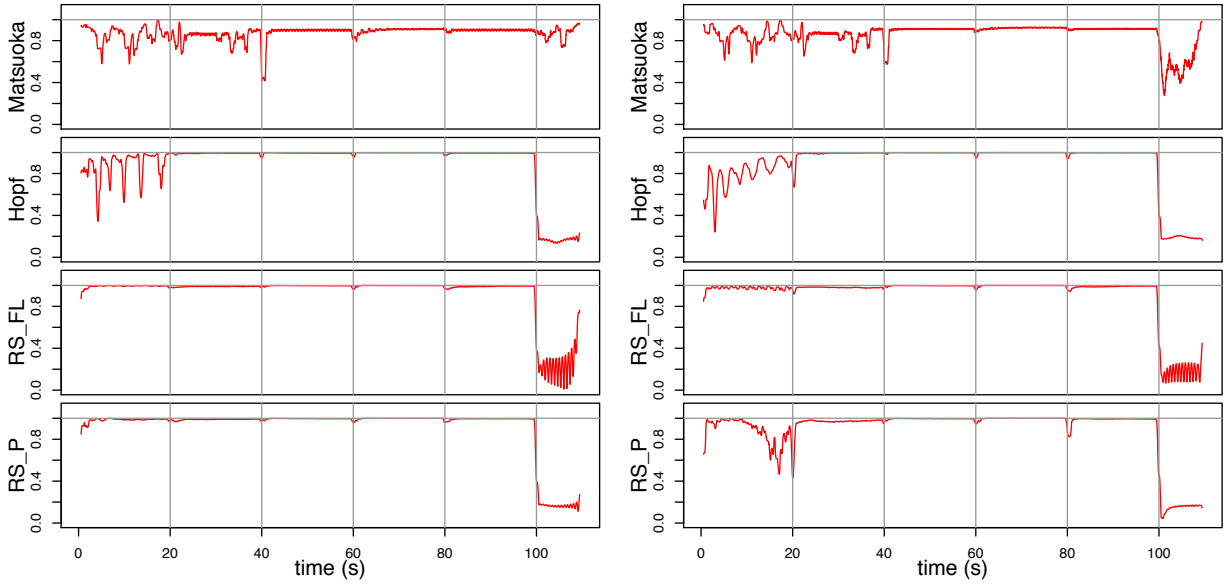
**Figure 10** Response of the Rowat-Silverston oscillator with Frequency Learning. In gray: CPG input, in black: CPG output for both joints



**Figure 11** Response of the Rowat-Silverston oscillator with all the plasticity mechanisms. In gray: CPG input, in black: CPG output for both joints

suited. Very few works undertook the oscillator comparison endeavour (Collins and Richmond, 1994). We, however, think that this is an important question as many models are available but each has its own strength and weaknesses and they may be suitable for different purposes. In this work, we arbitrarily chose the Matsuoka, Hopf and Rowat-Silverston models because we see them as complementary. Nevertheless, this work could be extended by integrating other models into the comparison, and also by testing other applications such as locomotion, rhythmic work tasks, rhythmic movements with no physical interaction and so on and so forth. In future works, it would also be interesting to

evaluate the impact of impedance control on the oscillators and particularly the feel of the interaction in human-robot physical interactions. We also expect the stiffness to influence the learning mechanisms, especially the adaptation speed.



**Figure 12** PLV for joint 2 (left), joint 3 (right). The vertical grey lines delimit each frequency range. The horizontal line indicates the reference for perfect coordination at 1.0

**Table 3** Synchrony frequency range where  $PLV \geq 0.95$  for each oscillator with plasticity.  $\Delta\omega_1$  and  $\Delta\omega_2$  define the frequency entrainment with plasticity and without plasticity

| Model                                     |            | $\omega_{intr}$<br>[Hz] | $\omega_{min}$<br>[Hz] | $\omega_{max}$<br>[Hz] | $\Delta\omega_1$ | $\Delta\omega_2$ |
|---|------------|-------------------------|------------------------|------------------------|------------------|------------------|
| Rowat-Silverston<br>Frequency<br>Learning | $\sigma_s$ |                         |                        |                        |                  |                  |
|   | 13         | 0.5                     | 0.1                    | 14.1                   | 14               | 13.7             |
|   | 50         | 1.0                     | 0.1                    | 18.6                   | 18.5             | 18.2             |
|   | 120        | 1.5                     | 0.1                    | 24.1                   | 24               | 23.5             |
|   | 200        | 2.0                     | 0.1                    | 29.2                   | 29.1             | 28.7             |
|   | 340        | 2.5                     | 0.1                    | 37.5                   | 37.4             | 36.6             |
|   | 490        | 3.0                     | 0.1                    | 46.6                   | 46.5             | 45.2             |
| Hopf<br>Frequency<br>Learning             | $\theta$   |                         |                        |                        |                  |                  |
|   | 3.5        | 0.5                     | 0.1                    | 13.6                   | 13.5             | 9.4              |
|   | 7          | 1.0                     | 0.1                    | 14.0                   | 13.9             | 9.7              |
|   | 10         | 1.5                     | 0.1                    | 14.2                   | 14.1             | 9.9              |
|   | 14         | 2.0                     | 0.1                    | 14.7                   | 14.6             | 10.2             |
|   | 16         | 2.5                     | 0.1                    | 14.9                   | 14.8             | 10.4             |
|   | 20         | 3.0                     | 0.1                    | 15.5                   | 15.4             | 10.7             |
| Matsuoka<br>$T, \tau$<br>Adaptation       | b          |                         |                        |                        |                  |                  |
|   | 3.5        | 0.5                     | 0.1                    | 10.1                   | 10.0             | 0.3              |
|   | 8          | 1.0                     | 0.2                    | 14.9                   | 13.7             | 0.3              |
|   | 13         | 1.5                     | 0.3                    | 13.6                   | 13.3             | 0.3              |

**Table 4** Average power  $\frac{1}{T_{max}} \sum |F_i(t) \cdot vel(t)|$  (Watt) applied to both joints using the various neural oscillators

| Model   | Joint 2 | Joint 3 |
|---|---------|---------|
| Rowat-Silverston                                      | 2.15    | 1.41    |
| Rowat-Silverston - $\sigma_s$ Learning                | 0.33    | 0.20    |
| Rowat-Silverston - $\sigma_s, A_f, \epsilon$ Learning | 0.23    | 0.10    |
| Hopf  | 1.12    | 1.07    |
| Hopf - $\theta$ Learning                              | 0.34    | 0.24    |
| Matsuoka  | 1.16    | 0.27    |
| Matsuoka - Time constants adaptation                  | 0.54    | 0.1     |

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